

Name Key

Review Trig Problems using Formula Sheet

1. Simplify: $\sin x \sec x \cot x$

$$\frac{\sin x}{\cos x} \cdot \frac{\cos x}{\sin x} = \boxed{1}$$

2. Simplify $\cos y(\tan y - \sec y)$

$$\cos y \left(\frac{\sin y}{\cos y} - \frac{1}{\cos y} \right) = \cos y \left(\frac{\sin y - 1}{\cos y} \right) = \boxed{\sin y - 1}$$

3. Simplify $(\sin^2 x)(\cos^2 x) + \cos^4 x$

$$\cos^2 x (\sin^2 x + \cos^2 x) \\ \cos^2 x (1) = \boxed{\cos^2 x}$$

$$\text{Prove: } \frac{1(1+\sec x)}{1-\sec x} + \frac{1(1-\sec x)}{1+\sec x} = -2 \cot^2 x$$

$$\frac{1+\sec x + 1-\sec x}{(1+\sec x)(1-\sec x)}$$

$$\frac{2}{1-\sec^2 x} = \frac{2}{-\tan^2 x} = \frac{2}{-\cot^2 x} = -2 \cot^2 x \checkmark$$

5. Prove the following identity: $\tan^2 x - \sin^2 x = (\sin^2 x)(\tan^2 x)$

$$\frac{\sin^2 x - \sin^2 x}{\cos^2 x}$$

$$\sin^2 x (\frac{1}{\cos^2 x} - 1)$$

6. Prove $\sin(x + \pi) = -\sin x$

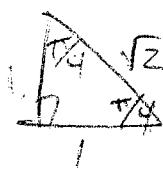
$$\begin{aligned} & \sin x \cos \pi + \cos x \sin \pi \\ & \sin x(-1) + \cos x(0) \\ & = -\sin x \checkmark \end{aligned}$$

$$\frac{1}{\cos^2 x} - \frac{\cos^2 x}{\cos^2 x}$$

$$\begin{aligned} & \sin x \cdot \frac{1-\cos^2 x}{\cos^2 x} \\ & \sin^2 x \cdot \frac{\sin^2 x}{\cos^2 x} \end{aligned}$$

$$= \sin^2 x \cdot \tan^2 x \checkmark$$

$$7. \text{ Find the exact value of } \cos \frac{7\pi}{12} = \frac{\pi}{12} + \frac{3\pi}{12} = \frac{\pi}{4}$$



$$\cos\left(\frac{\pi}{3} + \frac{\pi}{4}\right)$$

$$\cos \frac{\pi}{3} \cos \frac{\pi}{4} - \sin \frac{\pi}{3} \sin \frac{\pi}{4}$$

$$\left(\frac{1}{2}\right)\left(\frac{1}{\sqrt{2}}\right) - \left(\frac{\sqrt{3}}{2}\right)\left(\frac{1}{\sqrt{2}}\right)$$

$$= \frac{1}{2\sqrt{2}} - \frac{\sqrt{3}}{2\sqrt{2}}$$

$$= \boxed{\frac{1-\sqrt{3}}{2\sqrt{2}}}$$

$$8. \text{ Find the exact value of } \sin \frac{\pi}{12} = \frac{\pi}{2} - \frac{3\pi}{12}$$

$$\sin\left(\frac{\pi}{2} - \frac{3\pi}{12}\right)$$

$$\sin \frac{\pi}{3} \cos \frac{\pi}{4} - \cos \frac{\pi}{3} \sin \frac{\pi}{4}$$

$$\left(\frac{\sqrt{3}}{2}\right)\left(\frac{1}{\sqrt{2}}\right) - \left(\frac{1}{2}\right)\left(\frac{1}{\sqrt{2}}\right) = \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}} = \boxed{\frac{\sqrt{3}-1}{2\sqrt{2}}}$$

$$9. \text{ Find the exact value of } \tan \frac{5\pi}{12} = \tan\left(\frac{\pi}{6} + \frac{\pi}{4}\right)$$

$$\tan\left(\frac{\pi}{6} + \frac{\pi}{4}\right) = \frac{\tan \frac{\pi}{6} + \tan \frac{\pi}{4}}{1 - \tan \frac{\pi}{6} \tan \frac{\pi}{4}} = \frac{\frac{1}{\sqrt{3}} + 1}{1 - \left(\frac{1}{\sqrt{3}}\right)} = \frac{\frac{1+\sqrt{3}}{\sqrt{3}}}{\frac{\sqrt{3}-1}{\sqrt{3}}} = \boxed{\frac{1+\sqrt{3}}{\sqrt{3}-1}}$$

10. If the $\sin \theta = \frac{3}{8}$ and θ is in the first quadrant, what is $\sin(2\theta)$, $\cos(2\theta)$, and $\tan(2\theta)$?

$$\begin{array}{l} \text{Right triangle with legs 3 and 5. Hypotenuse is 8.} \\ x^2 + 3^2 = 8^2 \\ x^2 + 9 = 64 \\ x^2 = 55 \\ x = \sqrt{55} \end{array}$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\begin{aligned} &= 2\left(\frac{3}{8}\right)\left(\frac{\sqrt{55}}{8}\right) \\ &= \frac{3\sqrt{55}}{32} \end{aligned}$$

$$\cos 2\theta = 1 - 2\sin^2 \theta$$

$$\begin{aligned} &= 1 - 2\left(\frac{3}{8}\right)^2 \\ &= 1 - 2\left(\frac{9}{64}\right) = 1 - \frac{18}{64} = \frac{46}{64} = \frac{23}{32} \end{aligned}$$

$$\tan 2\theta = \frac{\tan \theta}{1 - \tan^2 \theta} = \frac{2\left(\frac{3}{\sqrt{55}}\right)}{1 - \left(\frac{3}{\sqrt{55}}\right)^2} = \frac{\frac{6}{\sqrt{55}}}{1 - \frac{9}{55}} = \frac{\frac{6}{\sqrt{55}}}{\frac{46}{55}} = \frac{330}{46\sqrt{55}}$$

11. Find $\cos 2A$ if $\tan A = -\frac{7}{24}$ and A is in quadrant II.

$$\begin{array}{l} \text{Right triangle with legs 7 and 24. Hypotenuse is 25.} \\ \text{Angle } A \text{ is in quadrant II.} \end{array}$$

$$2\cos^2 \theta - 1$$

$$2\left(\frac{-7}{25}\right)^2 - 1$$

$$2\left(\frac{49}{625}\right) - 1$$

$$= \frac{98}{625} - \frac{625}{625} = \boxed{\frac{-527}{625}}$$